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Thermodynamic law for adaptation of plants to environmental temperatures*

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Abstract: A thermodynamic law of adaptation of plants to temperature is developed. Plant growth rate is proportional to the product of the metabolic rate and the metabolic efficiency for production of anabolic products. Over much of the growth temperature range, metabolic rate is proportional to mean temperature and efficiency is proportional to the reciprocal of temperature variability. The mean temperature and short-term (hours to weeks) variability of temperature during the growth season at a particular location thus determine the optimum energy and growth strategy for plants. Because they can grow and reproduce most vigorously, plants with a growth rate vs. temperature curve that matches the time-at-temperature vs. temperature curve during the growth season are favored by natural selection. The law of temperature adaptation explains many recent and long-standing observations of plant growth and survival, including latitudinal gradients of plant diversity and species range.

Keywords: Species distribution; respiration; temperature; thermodynamics; adaptation; species richness; latitude.

INTRODUCTION

Thermodynamic analysis can provide valuable, and sometimes surprising, insights into even the most complex of systems. Thermodynamic consideration of the overall reactions of growth metabolism has, for example, provided a quantitative description of plant growth rate as a function of temperature from measurements of respiratory heat and CO_2 rates [1]. (Growth is used here to denote reproduction, development, and increase in body size, mass, or energy content.) Further consideration of the effects of temperature on rates and energy use efficiencies of growth metabolism in this paper leads to a quantitative description of the effects of environmental temperature on the growth of plants. The analysis here identifies the key environmental determinants of plant growth to be the mean temperature and the temperature variation during the growth season. Mean temperature affects reaction rates, whereas temperature variability affects metabolic energy use efficiency. Growth rate equals the product of metabolic rate and efficiency and therefore is proportional to the ratio of the climate variables, temperature and

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temperature variability. Our hypothesis is that these variables drive evolution of plant metabolism to optimize both growth rate and efficiency within the local pattern of environmental temperatures. Natural selection by temperature thus causes global, and delimits local, patterns of species distributions. We propose that the cause and effect relation between growth and the ratio of mean temperature to temperature variability derived from thermodynamic relations be called the law of temperature adaptation.

Combined with data on global temperatures, the law of temperature adaptation explains the existence of global-scale, latitudinal gradients in species density and range of plants. On a global scale, terrestrial species density decreases and species range increases with increasing latitude and elevation. These correlations are generally accepted despite studies with differing ecosystems, approaches, etc. [2-18]. These global-scale correlations presuppose the existence of a universal law, but no fundamental explanation has previously been given of how interactions between environmental variables and plant metabolism cause latitudinal gradients of species range and density. "Although a multitude of hypotheses have been proposed to explain this pattern there is little consensus upon their relative importance or critical data on the underlying causes" [18]. We propose that environmental temperature is the only environmental variable that changes systematically with elevation and latitude on a global scale and can be mechanistically linked to the biochemical reactions of growth. Environmental temperature is thus the fundamental cause of the global gradients in species range and density. Other variables such as energy availability, mutation rate, UV radiation, evapotranspiration, and energy flow cannot be fundamentally linked to metabolism by thermodynamic relations. Environmental variables such as water, fire frequency, and soil type also determine where a given species will or will not grow, but while these variables are vitally important at local scales, and many covary with local temperature variations, none change systematically on a global scale.

As a universal law, the law of temperature adaptation must apply to all organisms, but only terrestrial plant species are used as examples in this paper. This paper (1) discusses how environmental temperatures experienced by plants are structured in time; (2) develops a quantitative theory of how plant metabolism adapts to environmental temperature; (3) examines experimental support for predictions of the theory; (4) describes latitudinal trends in the ratio of mean temperature to temperature variability; and (5) examines global-scale gradients in range and density of plant species in light of the law of temperature adaptation and global temperature patterns.

STRUCTURE OF ENVIRONMENTAL TEMPERATURE

Figure 1 illustrates a pattern of continuously changing temperature as typically experienced by plants in temperate zones. The low for the three days covered in Fig. 1 was 14.1 °C, the high was 29.5 °C, and the mean was 22.0 °C. The 15.4 °C range in temperature is typical of daily temperature variation in inland temperate zones. An informative way to summarize environmental temperature data is as plots of the time spent at each temperature vs. the temperature, Fig. 2. Such plots show the time that a plant spends at each temperature, and thus the effect of the local temperature variation on growth. Three conclusions are apparent from this plot. First, mean temperature data clearly do not provide sufficient information for analyzing the relation between temperature and growth of ectotherms. Second, the distribution is distinctly bimodal. And third, the time at the mean temperature is small. Plants spend far more time growing at temperatures around 16 and 26 °C than at the mean temperature. Accumulation of data over longer periods, in which average temperatures shift with changing weather patterns and season, leads to plots of temperature distribution that disguise the diurnal temperature shift and appear to be unimodal, but the effects of daily temperature variation on plant growth remain. The widely reported maximum, minimum, and mean temperatures for a day, month, year, etc. are thus a very poor description of the temperatures experienced by plants, and correlation of plant growth with these temperature measures can be misleading.

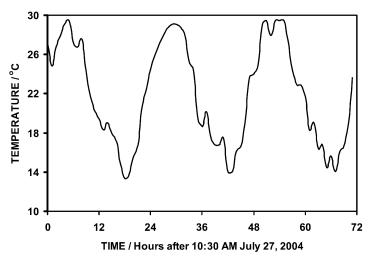


Fig. 1 Hourly temperatures through 27–29 July 2004 at Logan, UT, USA recorded with a HOBO Pro Series temperature logger from Onset Computer Corp., Bourne, MA.

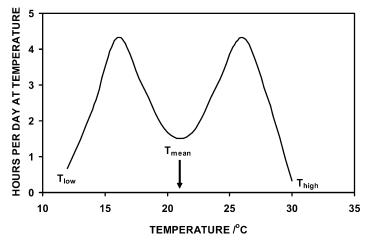


Fig. 2 Frequency plot (hours per day at each temperature vs. temperature) of environmental temperatures shown in Fig. 1.

For example, on a global scale, species range and density are correlated with annual mean temperatures. However, such correlations do not demonstrate cause and effect relations. This problem is evident in a recent paper by Allen et al. [16], who proposed a cause and effect relation between mean annual temperature and the global gradients of species richness based on the linearity of a log-inverse plot, i.e., "the relation between the natural logarithm of species richness and inverse absolute temperature is approximately linear." They then concluded that the gradient of mean annual temperature with latitudes causes the global gradient of species biodiversity. This conclusion is invalid for at least two reasons. First, even random data sets are linearized by this type of plot and thus mask the true relationship between variables. Second, mean annual temperature includes both times and temperatures during which growth is not possible, e.g., at 45° latitude, approximately half the year has temperatures that do not allow plant growth, and at 60° most of the temperatures included in the annual mean have no relevance to plant growth. Effects of temperature on plant distributions can only be analyzed in reference to times, seasons, and places when and where plants actually grow.

The thermally allowed growth season can be defined as the period of time in which most days have several hours above the freezing point of water. This varies from 52 weeks at low elevations near the equator to only 6 to 10 weeks in subpolar and alpine regions. At all elevations and latitudes in the Northern Hemisphere where plant growth is possible, the thermally allowed growth season includes significant portions of the months of June and July. Thus, values of daily maximum and minimum temperatures during June and July provide reasonable estimates of temperature and temperature variation during the growth season. Similarly, data for December and January are representative of growth temperatures in the Southern Hemisphere.

With these estimates, global patterns of terrestrial growth season temperature and temperature variation can be plotted as averages at each latitude. (This approach neglects the local effects of altitude, ocean currents, etc., but allows focus on average, global-scale effects. Altitude will be treated later in the discussion.) Figure 3 presents a plot of maximum high and minimum low temperatures for June and July in the Northern Hemisphere and for December and January in the Southern Hemisphere. Latitudes near $\pm 30^{\circ}$ experience higher temperatures during the growing season than either the tropics or the subpolar regions. Minimum temperatures plateau around the equator and decrease toward the polar regions. For example, plants growing during the Alaskan summer experience higher, as well as lower, temperatures than plants in lowland Costa Rica. Figure 3 also shows the difference between maximum and minimum temperatures during the growing season ($\Delta T_{\rm env}$). $\Delta T_{\rm env}$ increases rapidly from the equator to near 35° N latitude, then only slowly to about 70° N. Above 70°, $\Delta T_{\rm env}$ decreases rapidly. In the Southern Hemisphere, $\Delta T_{\rm env}$ increases rapidly to nearly 40° S, then decreases. The shape of the $\Delta T_{\rm env}$ curve suggests that $\Delta T_{\rm env}$ is an important variable determining species distribution. The curve of $T_{\rm mean}$ vs. latitude is approximately the average of the curves for the maximum and minimum shown in Fig. 3.

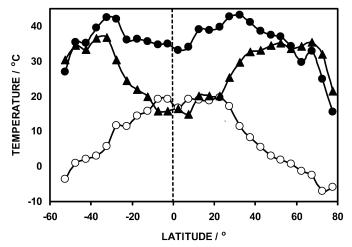


Fig. 3 Maximum (●) and minimum (○) temperatures and their difference (▲) for June and July in the Northern Hemisphere and for December and January in the Southern Hemisphere [46].

TEMPERATURE EFFECTS ON PLANT GROWTH

Some typical plant growth rate vs. temperature curves are shown in Fig. 4. Plant growth has high and low temperature limits as well as a (often broad) temperature optimum. Curves in Fig. 4 represent plants adapted to lowland tropics with warm, near constant temperatures, to temperate regions, and to high-latitude or high-elevation locations with very large temperature variations. Such curves, though tedious

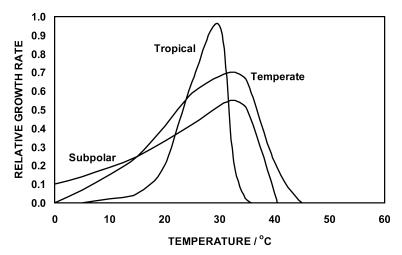


Fig. 4 Schematic plots of plant growth rate vs. temperature for plants adapted to near constant tropical temperatures to more variable temperate climate temperatures, and to highly variable subpolar temperatures.

to obtain by traditional means, can now be rapidly generated for individual plants or populations by calorespirometric measurements of heat and CO₂ rates on small, excised bits of growing tissue [19].

Plants well adapted to a site through long periods of natural selection have growth rate vs. temperature curves that closely match the temperature distribution plot (e.g., Fig. 2) during the growth season for that site [20–22]. Some plants even exhibit bimodal curves of growth rate vs. temperature that match the bimodal temperature frequency plots of the environment to which they are adapted [21,22]. Closely matched curves indicate a plant is spending much of the time during its growth season near its optimum growth temperature and all of its time within the temperature range allowing growth. Survival, growth, and reproduction of such plants are greatly enhanced relative to plants with temperature optima in a range encountered less often. Plants, of course, only grow at temperatures when other, local environmental variables (such as water and nutrients) are appropriate for the plant.

Relation between respiratory metabolism and growth

As suggested by Hoh and Cord-Ruwisch [23], it is necessary to consider the thermodynamics of growth and temperature responses to develop a correct biological model of the relations between environmental factors and growth and to identify the temperature functions that account for local and global scale distributions. We have developed the required thermodynamic model by expressing growth rate ($R_{\rm grow}$) as the product of metabolic rate (measured by the rate of ${\rm CO_2}$ production, $R_{\rm CO_2}$) and a function of the substrate carbon conversion efficiency (i.e., the fraction of substrate retained in anabolic products, ε), eq. 1 [1,24].

Growth rate (Cmole s⁻¹) =
$$R_{\text{grow}} = R_{\text{CO}_2} \left[\varepsilon / (1 - \varepsilon) \right]$$
 (1)

This relation can be derived directly from the equation for respiration-driven growth of plants,

$$C_{\text{substrate}}$$
+ (compounds and ions of N, P, K, etc.) + $yO_2 \rightarrow \varepsilon C_{\text{bio}}$ + $(1-\varepsilon) CO_2$ (2)

and has been shown to accurately predict relative growth rates of plants from calorespirometric measurements [20,25–31]. Both $R_{\rm CO_2}$ and ε are functions of temperature. These temperature responses are such that the $R_{\rm grow}$ function in eq. 1 produces the typical skewed bell-curve of $R_{\rm grow}$ vs. temperature such as those shown in Fig. 4.

Total growth over a season, G, is equal to the integral of eq. 1 over time

$$G = \int R_{\text{CO}_2} \left[\varepsilon / (1 - \varepsilon) \right] dt \tag{3}$$

To establish the link between physiological and temperature variables, eq. 1 must be written in terms of environmental temperature variables. The average rate of CO_2 production over the growth season is proportional to the mean kinetic temperature [32], $T_{\rm MK-CO2}$, and the efficiency function [ε /(1- ε)] is an inverse function of the temperature variability [33 and see Appendix]. Therefore, approximating $T_{\rm MK-CO2}$, with $T_{\rm mean}$ (on the Celsius scale) and temperature variability with $\Delta T_{\rm env}$, eq. 1 becomes

$$R_{\text{grow}} = c(T_{\text{mean}})[f(\Delta T_{\text{env}}^{-1})]$$
(4)

where c is a proportionality constant. Use of the Celsius scale for $T_{\rm mean}$ assumes that growth rate goes to zero at the freezing point of water; other reference temperatures for zero growth rate could be used as appropriate. And, with the same substitutions as above and with the length of the growth season as Δt ,

$$G = c(T_{\text{mean}})[f(\Delta T_{\text{env}}^{-1})]\Delta t$$
 (5)

Equations 4 and 5 establish a relation among growth and the elevation/latitude-dependent parameters; environmental temperature and growth season. Note that both the growth rate and total growth are proportional to the ratio of mean temperature to temperature variability.

Equations 4 and 5 state the law of adaptation of plants to environmental temperatures. The biochemical and thermodynamic basis for this law, and thus the reasons for calling it a law are given in the Appendix where the connection between environmental variables and cellular metabolism and thus to genetic adaptation is established.

EXPERIMENTAL TESTS OF THE DERIVED LAW

The above theory predicts plant distributions are related to the ratio of $T_{\rm mean}$ and an inverse function of $\Delta T_{\rm env}$ during the growth season. If the theory is correct, these temperature variables determine the respiratory characteristics of autochthonous plants, the respiratory characteristics determine survival at a given location, and since $T_{\rm mean}$ and $\Delta T_{\rm env}$ change systematically with altitude and latitude on a global scale, the environmental temperature determines the distribution of plants on a global scale. This section reviews some experimental tests of these predictions.

Plant respiratory metabolism varies systematically with altitude and latitude

Criddle et al. [34] examined the Arrhenius temperature coefficients for metabolic heat rate (μ_a) in rapidly growing tissues of three species of woody shrubs from an approximately 500-km north-south range in the Great Basin region of the United States. Values of μ_a were a linear function of the altitude and latitude from which the accessions originated. Because the plants tested were grown in a common garden, μ_a is clearly a genetically determined adaptation, not an acclimation. Low elevation and low latitude accessions had lower temperature coefficients. Also, measurements on over 50 congeneric pairs of other species of perennials showed that the plant from the more northerly latitude or higher elevation always had the smaller temperature coefficient. McCarlie et al. [21] showed subpopulations of cheatgrass (Bromus tectorum) from widespread areas of western North America have large, location-specific differences in temperature responses of metabolic rates, energy efficiency, and growth that match the temperature patterns during growth seasons at the different locations. Studies on eucalyptus from widespread locations in Australia yield similar conclusions [26,28,35]. Other studies following simply R_{CO_2} or R_{O_2} , though giving less well defined spatial dependencies, still show that respiratory properties vary systematically with climate of origin (e.g., [36]). Thus, the evidence is strong that there is a cause and effect relation between the temperature dependence of respiratory rates and the climate of the native geographic locations, which are in turn related to latitude and elevation.

$T_{\rm mean}/\Delta T_{\rm env}$ is the environmental temperature function to which plants are adapted

Related trees at different elevations

Church [37] tested the predicted inverse relation of growth to $\Delta T_{\rm env}$ with studies on growth of genetically related trees. Metabolic rate measurements were made on 17 half-sib families of 15-year-old *Pinus ponderosa* planted at each of four sites with different latitudes and elevations. Although the test sites are at different elevations, the mean temperatures during branch elongation growth are essentially the same at all sites. This results from growth later in the season at higher elevations. Because $T_{\rm mean}$ is a constant, if growth rates (metabolic rate times efficiency) are proportional to $T_{\rm mean}/\Delta T_{\rm env}$, relative growth rates at each site are predicted to be proportional to $1/\Delta T_{\rm env}$. Plots of $1/\Delta T_{\rm env}$ vs. growth rate (as height growth in 15 years) confirm this prediction (Fig. 5). Height decreases linearly with decreasing values of $1/\Delta T_{\rm env}$ ($R^2 = 0.96$ for 4 sites with 17 families). Growth rate of these trees is not correlated with any other known environmental variable other than weak correlations with variables that are co-correlated with $\Delta T_{\rm env}$. This study confirms that $\Delta T_{\rm env}$ is a key environmental variable linking metabolism with latitude and elevation. The linear relation between growth and $1/\Delta T_{\rm env}$ also shows the relation between $[\varepsilon/(1-\varepsilon)]$ and $\Delta T_{\rm env}$ used in deriving eqs. 4 and 5 is a simple first-order reciprocal.

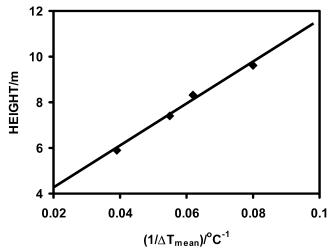


Fig. 5 Fifteen-year height growth of ponderosa pine half-siblings planted at four different elevations vs. the reciprocal of the temperature variation at the different sites during branch elongation [37].

The treeline boundary

Another test of the hypothesis that growth is proportional to $T_{\rm mean}/\Delta T_{\rm env}$ can be made using treeline temperature data. If the growth rate or annual growth is constant at treeline irrespective of species, latitude and elevation, and if efficiency is directly proportional to the reciprocal of $\Delta T_{\rm env}$, a plot of $T_{\rm mean}$ vs. $\Delta T_{\rm env}$ at the treeline is predicted to be a straight line (see eq. 5). Such a plot is shown in Fig. 6. The data produce a remarkably linear relation with the treeline value of $\Delta T_{\rm env}/T_{\rm mean}$ equal to 2.6. The linear relation again demonstrates the relation between $[\varepsilon/(1-\varepsilon)]$ and $\Delta T_{\rm env}$ in eqs. 4 and 5 is a simple first-order reciprocal. Note that points added to the plot using $T_{\rm mean}$ and $\Delta T_{\rm env}$ at locations that are either above or below treeline fall on one or the other side of the line with a rough relation between the distance from the line and distance from treeline (in units of elevation and latitude). The intercept is also essentially zero as required by eq. 5.

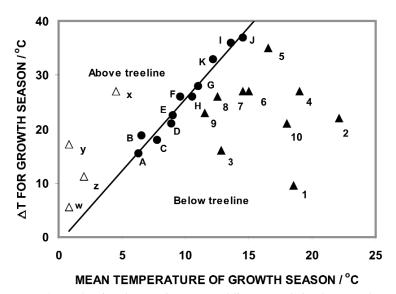


Fig. 6 Plot of $T_{\rm mean}$ vs. $\Delta T_{\rm env}$ showing the zero intercept and linear correlation between these two variables at treeline locations (\bullet). Non-treeline sites from equatorial to polar locations are shown by (\triangle). Treeline sites: A, Cruz Loma, Ecuador; B, Cotapaxi, Ecuador; C, Nara Moro, Mt. Kenya, Kenya; D, Mt. Wilhelm, Pinduande, New Guinea; E, Cotton Station, CA, USA; F, Dana Meadows, CA, USA; G, Lone Pine, CA, USA; H, Snow Flats, CA, USA; I, Bettles, AK, USA; J, near Ely, NV, USA; K, Bald Mtn., UT, USA. Above treeline sites: w, Gomessiat, Ecuador; x, Mt. Whitney, CA, USA; y, Teleki Valley, Mt. Kenya, Kenya; z, Summit Ridge, Mt. Wilhelm, New Guinea. Below treeline sites: 1, San Francisco, CA, USA; 2, Orange County, CA, USA; 3, upper Provo River Canyon, UT, USA; 4, Feather Falls, CA, USA; 5, Burney, CA, USA; 6, Allegheny, CA, USA; 7, Blue Canyon, CA, USA; 8, Fairbanks, AK, USA; 9, Inskip, CA, USA; 10, Davis, CA, USA. California temperature data are from the California Department of Water Resources database. Utah temperatures were collected in this study. Sources for the remainder are given in ref. [37].

Figure 7 shows how treeline elevations vary as a function of latitude in the Northern Hemisphere based on observed treeline elevations [38] and elevations calculated from $T_{\rm mean}$, $\Delta T_{\rm env}$, and latitude data [39]. Agreement between the experimental and calculated curves is remarkably good with the curve for experimental values slightly lower than calculated values. Environmental factors other than temperature may lower treeline elevations from the calculated elevation, but cannot raise them. Therefore, the small difference between the curves is in the correct direction and of reasonable magnitude.

The finding that $T_{\rm mean}/\Delta T_{\rm env}$ is a global constant for treelines generates a hypothesis that the ratio of mean environmental temperature to temperature variability will be a different, but constant, value at each of the boundaries between other life zones [40]. Further, this finding also supports our proposal that $T_{\rm mean}/\Delta T_{\rm env}$ explains the global-scale gradients in plant species range and density as functions of latitude and altitude.

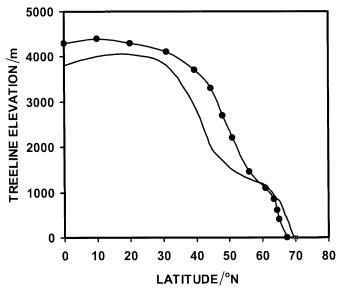


Fig. 7 Comparison of calculated (●) and measured (–) [38] treeline elevations as a function of latitude.

Survival, growth, and reproduction depends on close adaptation of plant metabolism to the pattern of environmental temperatures

Studies on eucalyptus clones and species, sagebrush, and redwood show that small differences in environmental temperature selectively favor growth of one plant over another as predicted by the law of temperature adaptation.

Eucalyptus clones

Large plantings of two closely related, rapid-growing clones of *Eucalyptus camadulensis* in an irrigated, well-managed, common garden in the Central Valley of California differed in growth from year to year. Calculations of growth rate vs. temperature based on calorespirometry measurements showed Simpson Timber Co. clone 4016 had a relatively narrow curve for growth rate vs. temperature with an optimum near 25 °C. Clone C11 had a broader curve with its optimum near 30 °C. Clone 4016 was calculated to be more efficient over a narrow range of temperatures. Clone C11, while less efficient over most of the temperature range, was predicted to be more efficient than 4016 at higher temperatures. These predictions were borne out by annual growth measurements. Clone C11 consistently outgrew clone 4016 during warmer years, yet was the slower of the two during cooler years. Total growth of the two clones over seven years was nearly equal. The different growth responses to temperature of these two clones were predicted by differences in responses of metabolic rate and efficiency to temperature [26].

Sagebrush

Two subspecies of sagebrush (*Artemisia tridentata* Nutt. ssp. *tridentata* Nutt. and A. *tridentata* Nutt. ssp. *vaseyana* [Rydb.] Beetle) and a stable hybrid swarm lying between the two occur naturally over an elevation gradient of only 85 m and a distance of only 1.1 km on an east-facing hillside near Nephi, Utah [41]. Three common gardens were established at the bottom, middle, and top of the site to test differences giving rise to this distribution. Plants in the three gardens and others recruited from proximal areas were reciprocally transplanted both lower and higher on the hillside. Transplanted plants fail to thrive and often die after one or two seasons. Though soil composition differed among sites, moving soil along with plants from one garden to another had no effect on these outcomes. The sites have been exhaustively analyzed for differences in herbivory, water, soil microbes, etc. with no significant difference found except in environmental temperature [42]. Temperature differences were small, but signifi-

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cant [43,44]. Differences occur in both mean temperatures and temperature variability. Corresponding differences in metabolic responses to temperature were found among the sagebrush subspecies and hybrids [43]. The results are consistent with the hypothesis that very small differences in temperature dependence of respiration can dictate success or failure of a subspecies or hybrid population and thereby determine their locations for successful growth.

Redwood growth and distribution

California coast redwoods (*Sequoia sempervirens*) have been studied extensively to establish relationships among respiration, growth rate, range, and temperature. The geographic origins of redwood seedlings collected from the length of the native range along the California and Oregon coasts (but grown in a common greenhouse) can be determined from measurements of the temperature dependence of the respiratory heat rate [25,45]. Trees from the more northern and more variable temperature end of the range have smaller temperature coefficients and are therefore less affected by temperature variability. Each population appears to be genetically adapted to the temperature pattern of its native climate. Such variation in genetically defined properties of metabolism allows a species range much greater than the allowed range of growth for a plant or population within the species.

Eucalyptus species studies

The relation predicted to exist among climate, respiration, and distribution has also been tested with Eucalyptus species (Fig. 8) (and other species [20]) from native climates with different $T_{\rm mean}$ and $\Delta T_{\rm env}$. Figure 8 shows plots of normalized growth rate (as $\Delta H_{\rm B}R_{\rm grow}$) calculated from measured respiration properties vs. temperature for individual trees of three Eucalyptus species. All were grown in, and therefore acclimated to, a common environment. The responses of the species to temperature and also the growth temperature ranges for the three species differ. The growth temperature ranges are consistent with the high and low temperatures at the native locations as indicated at the bottom of Fig. 8. This figure also makes the point that metabolism must be adapted to the absolute values of the extremes of the temperature range. Intra-species variation occurs among plants of each of these species, but intra-species differences are smaller than between species differences, making curves in Fig. 8 for individual plants good approximations of each species as a whole.

The experimental evidence presented above, and much more that is not discussed here, confirms that plants are adapted to the temperature function, $T_{\rm mean}/\Delta T_{\rm env}$, and shows that plants within each habitat are closely adapted to the microclimate of that habitat. For example, the data on ponderosa pine growth and treeline temperatures show the appropriate temperature function describing plant growth is a direct proportionality to $T_{\rm mean}$ and an inverse proportionality to the first power of $\Delta T_{\rm env}$. Also, data of the type in Fig. 8 on many species show that the high and low thresholds for growth of autochthonous plants match the maximum and minimum temperatures of the environment during the growth season. The next section shows quantitatively how $T_{\rm mean}/\Delta T_{\rm env}$ is related to altitude and latitude and thus leads to altitudinal and latitudinal gradients of species range and density.

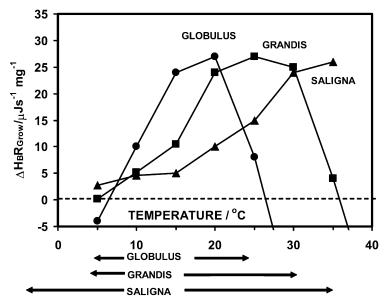


Fig. 8 Normalized rates of growth (as $\Delta H_{\rm B}R_{\rm grow}$, where $\Delta H_{\rm B}$ is the difference in the heats of combustion of carbohydrate and biomass) for three eucalyptus species (*Eucalyptus globulus* Labill, *E. grandis* W. Hill ex Maiden, *E. saligna* Sm.). Values were calculated from measurements of respiratory heat and ${\rm CO_2}$ production rates as a function of temperature. The environmental temperature range for growth of the species is given at the bottom of the figure.

LATITUDINAL TRENDS IN $T_{\rm mean}/\Delta T_{\rm env}$ AND $\Delta T_{\rm env}/T_{\rm mean}$

Figure 9 shows latitudinal patterns in $T_{\rm mean}/\Delta T_{\rm env}$ and $\Delta T_{\rm env}/T_{\rm mean}$ derived from climate data [46]. The curves are normalized to have $T_{\rm mean}/\Delta T_{\rm env}$ values of 1.0 at the equator. $\Delta T_{\rm env}/T_{\rm mean}$ is small at low latitude and large at high latitude, similar to species ranges. Values of the inverse ratio, $T_{\rm mean}/\Delta T_{\rm env}$, decrease slowly with increasing latitude in tropical regions, more rapidly near the edge of the tropical zone (about +24° and -15° latitude), then again more slowly to near the polar zones, similar to species densities.

Deviations from the average, global, latitudinal trends in these ratios exist owing to local geographical features such as mountains, proximity to oceans, etc. For example, mountainous locations cause wrinkles in the global contour maps of $\Delta T_{\rm env}/T_{\rm mean}$ and $T_{\rm mean}/\Delta T_{\rm env}$. The empirical "rule-of-thumb" that a 1° increase in latitude is approximately equivalent to 35-m increase in elevation in its effects on temperature can be used to estimate the size of the wrinkles. Table 1 shows the estimated, relative values of $\Delta T_{\rm env}/T_{\rm mean}$ in the Northern Hemisphere as both latitude and elevation change. Table 2 shows relative values of $T_{\rm mean}/\Delta T_{\rm env}$ as functions of both latitude and elevation.

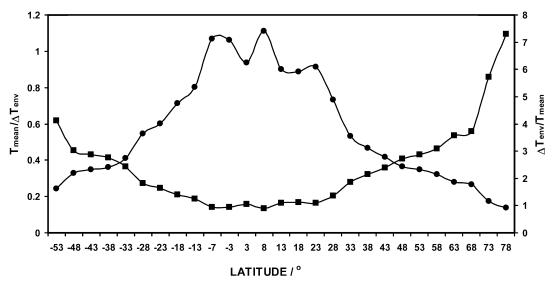


Fig. 9 $T_{\rm mean}/\Delta T_{\rm env}$ (ullet) and $\Delta T_{\rm env}/T_{\rm mean}$ (ullet) as functions of latitude. Positive latitude values indicate north and negative values south.

Table 1 The ratio, $\Delta T_{\rm env}/T_{\rm mean}$, as a function of latitude and elevation, calculated assuming 1° of latitude is equivalent to 35 m of elevation and normalized to unity at sea level at the equator.

Latitude/°N	Elevation/m									
	0	350	700	1050	1400	1750	2100	2450	2800	
0	1.0	1.1	1.3	1.5	1.9	2.4	3.2	4.4	6.1	
10	1.1	1.2	1.4	1.7	2.1	2.7	3.6	4.9	6.7	
20	1.3	1.4	1.7	2.0	2.5	3.2	4.3	5.8	8.1	
30	1.7	1.8	2.1	2.5	3.2	4.1	5.4	7.3	10.2	
40	2.2	2.4	2.7	3.3	4.2	5.4	7.1	9.6	13.4	
50	3.0	3.2	3.8	4.5	5.7	7.3	9.7	13.1	18.3	
60	4.2	4.2	5.3	6.4	8.0	10.3	13.7	18.6	25.8	
70	6.1	6.1	7.7	9.3	11.6	15.0	19.9	27.0	37.5	
80	9.2	10.0	11.5	13.9	17.4	22.8	29.7	40.3	56.0	

Table 2 The ratio, $T_{\rm mean}/\Delta T_{\rm env}$, as a function of latitude and elevation, calculated assuming 1° of latitude is equivalent to 35 m of elevation and normalized to unity at sea level at the equator.

	Elevation/m									
Latitude/°N	0	350	700	1050	1400	1750	2100	2450	2800	
0	1.00	0.92	0.80	0.66	0.53	0.41	0.31	0.23	0.16	
10	0.91	0.84	0.72	0.60	0.48	0.37	0.28	0.21	0.15	
20	0.76	0.70	0.60	0.50	0.40	0.31	0.23	0.17	0.12	
30	0.60	0.55	0.48	0.40	0.32	0.25	0.19	0.14	0.10	
40	0.46	0.42	0.36	0.30	0.24	0.19	0.14	0.10	0.07	
50	0.33	0.31	0.27	0.22	0.18	0.14	0.10	0.08	0.05	
60	0.24	0.24	0.19	0.16	0.12	0.10	0.07	0.05	0.04	
70	0.16	0.16	0.13	0.11	0.09	0.07	0.05	0.04	0.03	
80	0.11	0.10	0.09	0.07	0.06	0.04	0.03	0.02	0.02	

PATTERNS OF SPECIES DENSITY AND SPECIES RANGE ARISE FROM GRADIENTS IN $T_{\rm mean}/\Delta T_{\rm env}$ AND $\Delta T_{\rm env}/T_{\rm mean}$, RESPECTIVELY

As further explained in the Appendix, responses of physiological processes to environmental temperatures determine where a plant can grow. Natural selection leads to plants with an optimized product of respiration rate and efficiency and a growth temperature range that matches the range of environmental temperatures during the growth season. The nonequilibrium thermodynamic arguments in the Appendix show that plants can increase energy use efficiency by adaptation of energy metabolism to a narrowed range of environmental temperatures. However, this presents risk of death from loss of metabolic control during temperature events outside the range of adaptation [47–49]. In contrast, adaptation to a broader temperature range enhances the ability to survive at temperature extremes, but at the expense of reduced efficiency and therefore the ability to compete. Thus, natural selection balances these two adaptive forces, leading to plants with a growth curve that closely matches the local environmental temperature distribution.

The temperature adaptation law expressed in eqs. 4 and 5 together with natural selection by environmental temperature leads to the global pattern of species distribution [50]. Extension of Fig. 6, i.e., roughly a quadrangle formed by the treeline line shown and lines bounding areas on earth where plants grow, delimits the area (in T- ΔT coordinates) that allows growth. The areas in this quadrangle defined by populations of plants metabolically adapted to the same $\Delta T_{\rm env}$ and $T_{\rm mean}$ are variable. The size of the area is thus determined by the magnitude of the temperature range of the environment, $\Delta T_{\rm env}$ (see Fig 8). $\Delta T_{\rm env}$ equals both the temperature range of the environment and the temperature range for growth of a population of well-adapted plants (see Fig. 8, ref. [20], and the above paragraph). $\Delta T_{\rm env}$ is thus the variable metric of population or species range in T- ΔT coordinates. In T- ΔT coordinates, population (or species) area increases from the tropics to the poles, and because $\Delta T_{\rm env}$ also increases from the tropics to the poles, the observed geographic, global gradients of species density and range arise from the latitudinal dependence of the ratios, $T_{\rm mean}/\Delta T_{\rm env}$ and $\Delta T_{\rm env}/T_{\rm mean}$, respectively. These conclusions apply, regardless of the uncertainty in the definition of what constitutes a biological unit, e.g., population, subspecies, species, families or even ecosystems. As long as the definition is consistent, the $\Delta T_{\rm env}$ metric can be applied to populations, subspecies, species or other taxonomic groups.

Assuming the relations between species range and $\Delta T_{\rm env}/T_{\rm mean}$ and between species density and $T_{\rm mean}/\Delta T_{\rm env}$ are linear, then species density, defined as the number of species per unit area, is

species density =
$$N/A = c'(T_{\text{mean}}/\Delta T_{\text{env}})$$
 (6)

where N is the total number of species in area A and c' is a proportionality constant that depends on the taxon definition. Since the average species range is the area divided by the number of species in that area.

species range =
$$A/N = c''(\Delta T_{env}/T_{mean})$$
 (7)

Equations 6 and 7 predict curves of species range and density with latitude and are proportional to the curves in Fig. 9.

Adjustment for effects of area on species density

Before the predictions of eqs. 6 and 7 can be compared with observed trends, the predicted results may need to be corrected for the effect of variation of land area with latitude. The effect of land area may already be included in the temperature data shown in Fig. 9 because larger land areas include a wider range of values of $T_{\text{mean}}/\Delta T_{\text{env}}$ at a given latitude. But, assuming the effects of temperature and land area are independent, corrections can be estimated from land area as a function of latitude.

According to the general species-area relationship [2,14,17],

$$N = kA^{z} \tag{8}$$

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Values of z from 0.1 to 0.6 have been reported [17,51] with most commonly reported z values near 0.4 [12]. Figure 10 shows land areas as a function of latitude normalized to the area at the equator. Values from Fig. 10 were then used to calculate species density vs. latitude plots using eq. 8 with z=0.4 (Fig. 11, open symbols). These curves show that land area has little effect on the overall global patterns of latitudinal gradients of species density and range. Changes in z from 0.2 to 0.6 have small effects, reducing or increasing, respectively, the difference between the temperature-based curves of species density and the area-corrected curve.

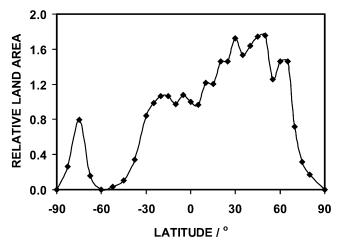


Fig. 10 Land area as a function of latitude from measurements of the combined lengths of land segments along latitudinal lines at 5° intervals. Northern Hemisphere latitudes are shown as (+) degrees and Southern Hemisphere latitudes as (-). See also [17], p. 285.

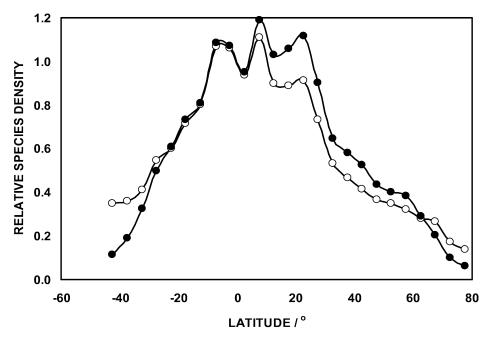


Fig. 11 Calculated average species density without (\bullet) and with (\bigcirc) correction for land area, plotted against latitude in the Northern (+) and Southern (-) Hemispheres. Values are normalized to give a value of 1.0 at the equator.

Comparison of predicted range and density with observations

The variation in species range and density predicted by Figs. 9 and 11 are in general agreement with direct observations of latitudinal changes in species range and density. For example, the prediction of a near two-fold decrease in species density from 12° to 45° north latitude indicated by Fig. 11 is close to reported values [9]. These results give general support to the equations derived above. The predictions of species range and density made with eqs. 6–8 are relative values. To apply the model to calculate real numbers for species densities and ranges, calibration constants using observed species numbers at many locations will be required. Such data on species numbers will also provide critical tests of the theory. Obtaining these, however, will not be easy. Among the problems is uncertainty in definitions of species and questions of whether the theory should more appropriately be framed in terms of other taxa.

CONCLUSIONS

The thermodynamic arguments presented here are generated from fundamental physical and physiological principles considering the thermodynamic effects of temperature and temperature variability on ectotherm energy use efficiency and metabolic rate, and therefore on productivity, as explained in the Appendix. Because the derivation is based on first principles, we refer to eqs. 4 and 5 as the law of temperature adaptation. This law applies universally to growth and distribution of ectotherms, and defines temperature conditions in which growth of a given organism can, but not necessarily will, occur. Ecologists have long asked "Are there general laws in ecology?" [52]. This paper defines such a law of ecology with a firm basis in thermodynamics and biochemistry.

The responses of physiological variables to temperature account for only one factor limiting ectotherm distribution. We recognize that modulators such as predation, symbionts, habitat variability, historical development, and scarcity of necessary resources (e.g., water or minerals) can prevent growth at any given location irrespective of favorable temperature conditions [14,53]. However, the law of temperature adaptation defines relative species range and density from fundamental thermodynamic principles, physiology of energy metabolism, and global patterns of climate that are inescapably superimposed on all local and historical determinants of the existence of a species at a particular location.

A perfect adaptation of plants to temperature is not possible because climate at any site varies from year to year. There is, thus, no single "best" solution for adaptation of energy metabolism and growth rate to a location. Organisms (both within and between species) with a range of properties exist at all sites, some better at growth and overcoming competition, others better at survival through climatic extremes. The weather "tomorrow" determines which is more fit. The relation between metabolic properties and location is further complicated because plants may also alter their effective environmental growth temperatures simply by altering the time during the season when growth occurs. Such responses add a "fuzziness" to the patterns of species range and density, but in all cases, growth remains subject to the limitations imposed by $T_{\rm mean}$ and $\Delta T_{\rm env}$ at the time of growth.

While answering important how and why questions of global gradients of species range and density, the law of temperature adaptation also provides a theoretical basis to correct for elevation differences, temperature-moderated regions, etc., locally altering the global pattern. The law of temperature adaptation, together with physiological measurements, can be employed to predict relative productivity of cultivars when used for agriculture or forestry in a particular climate, or to determine a most suitable climate for optimum productivity [54]. One only need measure (or for managed environments, set) the temperature distribution curve for a site during the growing season and the growth rate vs. temperature curve for the genotype. The more closely these two curves match, the more productive the genotype will be in the environment at the site. Integration of the growth rate curve over the temperature distribution during the growth season allows quantitative comparison of growth of different genotypes. If our hypothesis is correct that the ratio of mean temperature to temperature variability is constant at boundaries

between life zones, it could be used to predict how climate change will affect the distribution of ectotherms.

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APPENDIX: BIOMECHANICAL AND THERMODYNAMIC BASES FOR THE LAW OF ADAPTATION TO ENVIRONMENTAL TEMPERATURES

Relation between efficiency (ε) and temperature variability

Definition of the relations between plant metabolism and distribution (elevation/latitude) and temperature requires understanding the relation between the substrate carbon conversion efficiency, ε , and temperature. The assumption that ε decreases with increasing temperature variation (i.e., that $[\varepsilon l(1-\varepsilon)]$ is an inverse function of ΔT) is validated by the second law of thermodynamics, which requires that mass and energy flow through the system described by eq. 2 must be accompanied by heat transfer from the system to the surroundings [55–58]. The relation between the magnitude of the heat loss per unit of biomass produced and variability of conditions is given by the theorem of minimal entropy production at steady state [33]. This theorem states that, for any reaction sequence, the steady state is characterized by a minimum rate of entropy production. Any displacement from steady state, i.e., variable reaction conditions such as $\Delta T_{\rm env}$, results in an increased energy loss to the environment for a given amount of reaction.

The requirement for ε to vary with variable conditions can also be understood from consideration of the biochemistry of respiration. Plant growth requires respiration of a fraction of the products from photosynthesis to produce CO_2 and energetic intermediates (largely ATP and NADH) that are subsequently used in anabolic reactions for conversion of additional substrate into plant biomass. The overall reaction for aerobic growth of plants (eq. 2) is thus the sum of the catabolic reaction

$$C_{\text{substrate}} + yO_2 + \text{nADP} + \text{nPi} + \text{aNAD}^+ \rightarrow CO_2 + \text{nATP} + \text{aNADH} + \text{aH}^+$$
(9)

and the anabolic reaction

$$\begin{aligned} &C_{substrate} + x (compounds \ and \ ions \ of \ N, \ P, \ K, \ etc.) + mATP + bNADH + bH^+ \rightarrow \\ &C_{bio} + mADP + mPi + bNAD^+ \end{aligned} \tag{10}$$

For plants, $C_{substrate}$ in these equations represents photosynthate (carbohydrate) and C_{bio} is used to indicate all carbon in anabolic products.

Reactions 9 and 10 occur in the condition-dependent ratio $(1-\varepsilon)/\varepsilon$. The two reactions are energy-coupled through cyclic production and hydrolysis of ATP and redox cycling of NADH. However, they are not stoichiometrically coupled [59]. Because the rates of reactions 9 and 10 have different dependencies on temperature and other reaction conditions, the pairs of coefficients n and m, and a and b, respectively for the two reactions, are generally not equal and vary with conditions, i.e., there is variable stoichiometry between anabolism and catabolism. As a consequence, substrate carbon conversion efficiency varies with temperature and other changing reaction conditions.

Requirement for maintaining near constant phosphorylation potential while ε varies, the role of futile cycles

Unequal and changing relative rates of reactions 9 and 10 for formation and use of ATP and NADH as reaction conditions change cannot be allowed to significantly alter [ATP]/[ADP] ratios because survival of all active organisms requires cellular redox and phosphorylation potentials (or free energy change for hydrolysis of ATP) to remain in a narrow range [58–62]. Maintaining ATP/ADP ratios in varying temperature conditions is a major problem because adenine nucleotide concentrations in the cell are only millimolar, while turnover of ATP is very rapid. One gram of meristematic tissue of actively growing plants produces (and hydrolyzes) approximately 1 g of ATP each day. Loss of control of the phosphorylation potential when temperatures exceed the range to which the plant is adapted lead to chilling or heat shock responses such as loss of membrane integrity and electrolyte leakage [20].

To maintain the cellular phosphorylation potential nearly constant, reaction 9 must always produce ATP and NADH at rates equal to or in excess of their rates of use in the biosynthetic reactions of

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reaction 10 (i.e., $n \ge m$ and $a \ge b$). If ATP is synthesized slower than it is used, the phosphorylation potential falls (degree of coupling decreases) and cell death eventually would ensue. If ATP is synthesized faster than it is used for biosynthesis, the excess can be disposed of by hydrolytic reactions. The balance between the rates of ATP synthesis and use is maintained by condition-dependent "futile" uncoupled hydrolysis of ATP or equally "futile" reactions that decrease the rate of ATP synthesis by short-circuiting electron transport [22,63,64]. The overall result is a condition-dependent energy loss, a variable coupling between catabolic and anabolic processes, and a condition-dependent ratio of energy loss to growth. Plants adapted to, and growing in, climates with large variations in reaction conditions must "waste" more energy to maintain phosphorylation potentials over a wider range than narrowly adapted plants. Thus, the larger $\Delta T_{\rm env}$, the lower the energy use efficiency.

A thermodynamic requirement for the engagement of futile pathways for optimizing coupling of substrate oxidation and phosphorylation in changing reaction conditions has been demonstrated from considerations of linear nonequilibrium thermodynamics [55,65–67]. Stucki [61] provided evidence that it is correct to apply the theorem of minimal entropy production to steady state oxidative phosphorylation (also see [68]) and demonstrated linear force-flow relations in oxidative phosphorylation in mitochondria. Various workers [54,68] have confirmed that these concepts also apply generally to growth of cells under near steady-state conditions and have used measurements of heat dissipated as an indication of the increase in entropy during variable growth conditions. They showed that variation in reaction conditions around steady state or a displacement to a higher steady-state rate results in increased heat loss per unit of biomass produced. Thermodynamic arguments thus require, and experimental studies show, that efficiency decreases as ΔT_{env} increases. To maintain phosphorylation potentials, ATP synthesis must be partially uncoupled or some ATP must be hydrolyzed without coupling to anabolic reactions. The amount of "wasted" ATP must be coordinated with the changes in environmental conditions to ensure equality of the overall rates of synthesis and hydrolysis of ATP. The condition-dependent waste of ATP reduces the substrate carbon conversion efficiency, but thereby maintains cell viability. Several sources infer (but do not rigorously prove for biological systems) that the larger and more frequent the variations perturbing steady state growth, the greater the energy loss from the system [69,70].